

# Test z aritmetiky 1

Cermat 2016 PId (14b)

$$\text{a) } 1 - \sqrt{\frac{25}{64}} = 1 - \frac{5}{8} = \frac{8}{8} - \frac{5}{8} = \underline{\underline{\frac{3}{8}}}$$

$$\text{b) } 5 + 3 \cdot (-2) - \underbrace{(5 + 2 \cdot 2)}_6 = 5 - 6 - 6 = \underline{\underline{-7}}$$

$$\text{c) } 3 \cdot \frac{2}{15} + \frac{1}{3} \cdot \frac{2}{15} = \frac{3 \cdot 2}{3 \cdot 15} + \frac{2}{45} = \frac{18}{45} + \frac{2}{45} = \frac{20}{45} = \underline{\underline{\frac{4}{9}}}$$

$$\text{d) } \frac{2 \cdot \frac{2}{3} - \frac{5}{6}}{\frac{2}{3}} = \frac{\frac{4}{6} - \frac{5}{6}}{\frac{2}{3}} = \frac{-\frac{1}{6}}{\frac{2}{3}} = -\frac{1}{6} : \frac{2}{3} = -\frac{1}{6} \cdot \frac{3}{2} = \underline{\underline{-\frac{1}{4}}}$$

Zjednoduř

**VZOREC**

$$\text{e) } (x+2)^2 + (x-2)(x+2) = x^2 + 4x + 4 + x^2 - 4 = 2x^2 + 4x$$
$$(x+2)(x+2) = x^2 + 2x + 2x + 4 = x^2 + 4x + 4$$
$$(x-2)(x+2) = x^2 - 2x + 2x - 4 = x^2 - 4$$

$$\text{f) } y(3y-1) - 3(y^2-y) = 3y^2 - y - 3y^2 + 3y = \underline{\underline{2y}}$$

Řeř rovnici:

$$\text{g) } \frac{1-x}{2} = 4-x + \frac{5x}{3} \quad / \cdot 6$$

$$3 - 3x = 24 - 6x + 10x$$

$$3 - 3x = 24 + 4x$$

$$-3x - 4x = 24 - 3$$

$$-7x = 21 \quad / : 7$$

$$-x = 3 \quad / \cdot (-1)$$

$$x = -3$$

$$\begin{array}{r} 0,06 \\ \cdot 0,5 \\ \hline 0,030 \end{array} \quad \begin{array}{r} 0,90 \\ - 0,03 \\ \hline 0,87 \end{array}$$

a)  $0,5 \cdot 0,06 - 0,09 : 0,1 = 0,03 - 0,9 = -0,87$   
 $L > 0,9 : 1$

b)  $(9 - \sqrt{9})^2 - (\sqrt{9})^2 = (9 - 3)^2 - (3)^2 = (6)^2 - 9 = 36 - 9 = 27$

c)  $\rightarrow 2 = \frac{4}{2}$   
 $\frac{2 - \frac{3}{5} \cdot \frac{5}{2}}{2} = \frac{\frac{4}{2} - \frac{3}{2}}{2} = \frac{\frac{1}{2}}{2} = \frac{1}{2} : 2 = \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$

d)  $\frac{3}{4} \cdot \frac{15}{2} - \left(\frac{3}{5}\right)^2 = \frac{3}{4} \cdot \frac{2}{15} - \frac{9}{25} = \frac{1}{10} - \frac{9}{25} = \frac{5}{50} - \frac{18}{50} = -\frac{13}{50}$

Zjednoduř

e)  $(2x-3)^2 + (12x-2x^2) = 4x^2 - 12x + 9 + 12x - 2x^2 = 2x^2 + 9$   
 $(2x-3)(2x-3) = 4x^2 - 6x - 6x + 9$

f)  $(2+y)(y-2) - 2(y^2-1) = y^2 - 4 - 2y^2 + 2 = -y^2 - 2$   
 $2y - 4 + y^2 - 2y$

Řeř rovnici:

g)  $\frac{6+5x}{6} - \frac{1}{3} = \frac{10}{9}x + 1 \quad / \cdot 18$

$$18 + 15x - 6 = 20x + 18$$

$$15x + 12 = 20x + 18$$

$$15x - 20x = 18 - 12$$

$$-5x = 6$$

$$5x = -6 \quad / : 5$$

$$x = -\frac{6}{5}$$

Test z aritmetiky 3

Cermat 2017 PID (14b)

$$a) 40 - 20 \cdot (-6) : 4 - 5 \cdot (4 + 12 : 4) = 40 + 120 : 4 - 35 = 40 + 30 - 35 = \underline{\underline{35}}$$

$$b) \frac{0,3^2}{0,1} : 0,01 = \frac{0,09}{0,1} : 0,01 = 0,9 : 0,01 = 90 : 1 = \underline{\underline{90}}$$

$$\hookrightarrow 0,09 : 0,1 = 0,9 : 1 = 0,9$$

$$c) \frac{7}{12} - \frac{5}{8} \cdot 1,6 = \frac{7}{12} - \frac{5}{8} \cdot \frac{16}{10} = \frac{7}{12} - \frac{2}{2} = \frac{7}{12} - \frac{12}{12} = -\frac{5}{12}$$

$$d) \frac{2\frac{2}{3} - 1\frac{3}{5}}{2\frac{2}{3}} = \frac{\frac{8}{3} - \frac{8}{5}}{\frac{8}{3}} = \frac{\frac{40-24}{15}}{\frac{8}{3}} = \frac{16}{15} = \frac{16}{15} \cdot \frac{3}{3} = \frac{2}{5}$$

Zjednoduř

$$e) (3a+1)^2 - 3a(2+5a) = \overbrace{3a^2 + 6a + 1}^{\text{VZOREC}} - 6a - 15a^2 = -6a^2 + 1$$

$$\hookrightarrow (3a+1)(3a+1) = 3a^2 + 3a + 3a + 1$$

$$f) (1+2b) \cdot \frac{b}{2} - \frac{2-b}{2} = \frac{(1+2b) \cdot b}{2} - \frac{2-b}{2} = \frac{b+2b^2-(2-b)}{2} = \frac{b+2b^2-2+b}{2} = \frac{2b^2+2b-2}{2} = \frac{2 \cdot (b^2+b-1)}{2} = b^2+b-1$$

Řeř rovnici:

$$g) x = 2,5 \cdot x$$

$$0 = 2,5x - x$$

$$0 = 1,5x \quad /: (1,5)$$

$$\underline{\underline{0 = x}}$$

Řeř rovnici:

$$h) (1-x) \cdot \frac{5}{6} = \frac{10}{9}x - \frac{1}{3} \quad /: 18$$

$$(1-x) \cdot 15 = 20x - 6$$

$$\frac{5}{6} - \frac{5}{6}x = \frac{10}{9}x - \frac{1}{3} \quad /: 18$$

$$15 - 15x = 20x - 6$$

$$-35x = -21 \quad /: (-1)$$

$$35x = +21 \quad /: 7$$

$$5x = 3 \quad /: 5$$

$$x = \frac{3}{5}$$

$$\text{a) } \sqrt{4 \cdot 0,25} = \sqrt{1} = 1$$

$$= 2 \cdot 0,5 = 1$$

$$\text{b) } 1:0,2^2 = 1:0,04 = \overset{\cdot 100}{100:4} = 25$$

$$\text{c) } 0,2: \frac{27}{25} - \frac{2}{3} = \frac{2}{10} \cdot \frac{25^5}{27} - \frac{2 \cdot 3}{3 \cdot 3} = \frac{5}{27} - \frac{18}{27} = -\frac{13}{27}$$

$$\text{d) } \frac{\frac{1}{5} - \frac{3}{10} + \frac{1}{4} \cdot 2^1}{4} = \frac{\frac{2}{10} - \frac{3}{10} + \frac{5}{10}}{4} = \frac{\frac{4}{10}}{4} = \frac{4}{10} : 4 = \frac{1}{10} \cdot \frac{1}{4} = \frac{1}{40}$$

Zjednoduř

$$\text{e) } (a+a) \cdot (1-a) - a \cdot a = 2a \cdot (1-a) - a^2 = 2a - 2a^2 - a^2 = 2a - 3a^2$$

$$\text{f) } \frac{n-1}{2} - \frac{2n-3}{4} = \frac{2 \cdot (n-1)}{2 \cdot 2} - \frac{2n-3}{4} = \frac{2n-2 - (2n-3)}{4} = \frac{2n-2-2n+3}{4} = \frac{1}{4}$$

Řeř rovnici:

$$\text{g) } -\frac{2}{3} \cdot \frac{x}{2} = \frac{5}{12}$$

$$-\frac{x}{3} = \frac{5}{12} \quad / \cdot 3 \quad \frac{5}{12} \cdot 3^1$$

$$-x = \frac{5}{4}$$

$$x = -\frac{5}{4}$$

Řeř rovnici:

$$\text{h) } \frac{x-2}{2} - x = 2 - \frac{2x}{3} \quad / \cdot 6$$

$$3x - 6 - 6x = 12 - 4x$$

$$-6 - 3x = 12 - 4x$$

$$-3x + 4x = 12 + 6$$

$$\underline{\underline{x = 18}}$$

a)  $0,5 : 0,5^2 = 0,5 : 0,25 = 50 : 25 = \underline{2}$

b)  $6 \cdot \frac{-15 - 6 \cdot (-2)}{2} = 6 \cdot \frac{-15 + 12}{2} = 6 \cdot \frac{-3}{2} = \underline{-9}$   
 $\hookrightarrow 3 \cdot [-15 - 6 \cdot (-2)] = 3 \cdot [-15 + 12] = 3 \cdot [-3]$

c)  $2 - \frac{1}{3} - \frac{1}{6} \cdot \frac{16}{3} = \frac{18}{9} - \frac{3}{9} - \frac{8}{9} = \frac{7}{9}$   
 $\hookrightarrow \frac{8}{9}$

d)  $\frac{7}{10} - \frac{2}{5} \cdot \frac{1}{10} = \frac{7}{10} - \frac{2 \cdot 1}{5 \cdot 10} = \frac{7}{10} - \frac{2}{50} = \frac{7}{10} - \frac{4}{10} = \frac{3}{10} = \frac{33}{10} : 11 = \frac{3}{10} : 3 = \frac{1}{10}$   
 $\frac{7}{10} - \frac{2}{5} \cdot \frac{1}{10} = \frac{7}{10} - \frac{2 \cdot 1}{5 \cdot 10} = \frac{7}{10} - \frac{2}{50} = \frac{7}{10} - \frac{4}{10} = \frac{3}{10} = \frac{33}{10} : 11 = \frac{3}{10} : 3 = \frac{1}{10}$   
 Minus bude až do konce

Zjednoduš

e)  $(x-4)^2 + (8-2x) \cdot 2x = x^2 - 8x + 16 + 16x - 4x^2 = -3x^2 + 8x + 16$   
 $\hookrightarrow \text{VZOREC } (x-4)(x-4) = x^2 - 4x - 4x + 16$

f)  $(3a + 2a) \cdot (a - 2a) - (a - 2a) = 3a \cdot (-a) - (-a) = -3a^2 + a$

Řeš rovnici:

g)  $4x + 1 = 4 \cdot (4x + 0,25)$

$$\begin{aligned} 4x + 1 &= 16x + 1 \\ 4x - 16x &= 1 - 1 \\ -12x &= 0 \quad /: (-12) \\ \underline{x} &= \underline{0} \end{aligned}$$

Řeš rovnici:

h)  $\frac{x-5}{2} + x = \frac{2x}{3} - \frac{5}{6} \quad /: 6$   
 $6 \cdot \frac{x-5}{2} = 4x$

$$\begin{aligned} 3x - 15 + 6x &= 4x - 5 \\ 9x - 15 &= 4x - 5 \\ 9x - 4x &= -5 + 15 \\ 5x &= 10 \quad /: 5 \\ x &= 2 \end{aligned}$$

$$\frac{9}{5} : 3 = \frac{9}{5} \cdot \frac{1}{3} = \frac{3}{5}$$

a)  $2 - 2 \cdot \frac{9}{3} = 2 - 2 \cdot \frac{3}{5} = 2 - \frac{6}{5} = \frac{10}{5} - \frac{6}{5} = \frac{4}{5}$

$2 - \frac{2 \cdot \frac{9}{3}}{3} = 2 - \frac{18}{3} = 2 - \frac{18}{5} : 3 = 2 - \frac{6}{5}$

b)  $\frac{3^2}{5} - \frac{3}{5^2} + \left(-\frac{3}{5}\right)^2 = \frac{5 \cdot 9}{5 \cdot 5} - \frac{3}{25} + \frac{9}{25} = \frac{45}{25} - \frac{3}{25} + \frac{9}{25} = \frac{51}{25}$

$$\left(-\frac{3}{5}\right)\left(-\frac{3}{5}\right) = +\frac{9}{25}$$

Zjednoduř

c)  $[(a-4a)^2 - 3a(3a+2)]^2 = [9a^2 - 9a^2 - 6a]^2 = [-6a]^2 = 36a^2$

$\downarrow$   
 $(-3a)^2 = (-3a)(-3a) = 9a^2$

d)  $(2b+1)(2b-1) - b(-b+b) + 1 = 4b^2 - 1 - 0 + 1 = 4b^2$

$\hookrightarrow$  vzorec:  $4b^2 - 1$   
 $\hookrightarrow$  rozdíl:  $4b^2 + 2b - 2b - 1$   
 $-b \cdot 0 = 0$

Řeř rovnici:

e)  $\frac{5x-2}{4} = 1,25x - \frac{1}{2} \quad /:4$

$$\frac{1,25}{-4} \quad \frac{5,00}{5,00}$$

$$5x - 2 = 5x - 2$$

$$0 = 0$$

NEKONEČNO DŘEŘENÍ ! Musí být zdvřr

Řeř rovnici:

f)  $\frac{2}{3} \cdot (x+1) = -\frac{1}{3} \cdot (2x-1) - 1 \quad /:3$

~~$\cdot \frac{3}{2} \cdot (x+1)$  ?~~

$$\frac{2}{3}x + \frac{2}{3} = -\frac{2}{3}x + \frac{1}{3} - 1 \quad /:3 \quad 2 \cdot (x+1) = -(2x-1) - 3$$

$$2x + 2 = -2x + 1 - 3$$

$$2x + 2 = -2x - 2$$

$$2x + 2x = -2 - 2$$

$$4x = -4 \quad /:4$$

$$\underline{\underline{x = -1}}$$

# Test z aritmetiky 7

Cermat 2017 PDD (14b)

Doplň čísla aby platila rovnost

$$12y : 2y = 6$$

a)  $(y + 6) \cdot (2y + 3) = 2y^2 + 15y + 18$   
 $2y^2 + 3y + 12y$

Vypočítej:

b)  $\left(\frac{11}{5} \cdot \frac{7}{20} - \frac{5 \cdot 7}{5 \cdot 20}\right) : \frac{7}{5} = \left(\frac{77}{100} - \frac{35}{100}\right) : \frac{7}{5} = \frac{42}{100} : \frac{7}{5} = \frac{42}{100} \cdot \frac{5}{7} = \frac{3}{10}$

c)  $\frac{3^2 - 3 \cdot 3}{9} + \frac{3}{1 + \frac{1}{3}} \cdot \frac{4 \cdot \frac{1}{3}}{6} = \frac{0}{9} + \frac{3}{\frac{4}{3}} \cdot \frac{\frac{4}{3}}{6} = \frac{1}{2}$   
 $\hookrightarrow \frac{\frac{4}{3}}{\frac{3}{4}} = \frac{4}{3} : \frac{3}{4} = \frac{4}{3} \cdot \frac{4}{3} = \frac{16}{9}$   
 $\hookrightarrow \frac{3}{\frac{3}{4}} = \frac{3}{3} \cdot \frac{4}{4} = 3 \cdot \frac{4}{4} = 3 \cdot 1 = 3$

Zjednoduš

d)  $(2a + \sqrt{25-16}) \cdot (2a - \sqrt{4+4+1}) = (2a+3) \cdot (2a-3) = 4a^2 - 9$   
 $\hookrightarrow \text{VZOREC}$   
 $\hookrightarrow \text{roz: } 4a^2 - 6a + 6a - 9$

Vypočítej:

e)  $(50 + \sqrt{2000}) \cdot (50 - \sqrt{2000}) = 50^2 - (\sqrt{2000})^2 = 2500 - 2000 = 500$   
 $2500 - 50 \cdot \sqrt{2000} + 50 \cdot \sqrt{2000} - 2000 = 2500 - 2000 = 500$

Řeš rovnici:

f)  $\frac{6x-5}{3} = 2x - \frac{10}{3} \quad / \cdot 3$

$6x - 5 = 6x - 10$   
 $6x - 6x = -10 + 5$   
 $0x = -5$   
 $0 \neq -5$   
**NEMÁ ŘEŠENÍ**

Řeš rovnici:

g)  $2 \cdot \frac{x-1}{9} - \frac{2x+3}{6} = \frac{1}{2} \quad / \cdot 18$

$4x - 4 - 6x - 9 = 9$   
 $-2x = 9 + 13$   
 $-2x = 22 \quad / : (-2)$   
 $x = -11$

$2 \cdot \frac{x-1}{3} = \frac{2 \cdot (x-1)}{3} = \frac{2x-2}{3}$

$\frac{2x-2}{3} - \frac{2x+3}{6} = \frac{1}{2} \quad / \cdot 18$

$2 \cdot (2x-2) - 3 \cdot (2x+3) = 9$   
 $4x - 4 - 6x - 9 = 9$   
 $-2x - 13 = 9$   
 $-2x = 9 + 13$   
 $-2x = 22 \quad / : (-2)$   
 $x = -11$

# Test z aritmetiky 8

Cermat 2018 PAD (14b)

a)  $\sqrt{1^2 - 0,6^2} = \sqrt{1 - 0,36} = \sqrt{0,64} = 0,8$

↳ NEPOHU ODMOCŇOVAT  
KAŽDÝ ZVLÁŠT!

b)  $100 - \frac{1}{0,01 \cdot 0,1} = 100 - \frac{1}{0,001} = 100 - 1000 = -900$

↳  $1 : 0,001 = 1000 : 1 = 1000$

c)  $\frac{\frac{4}{1+2} - 1}{1+2} = \frac{\frac{4}{3} - \frac{3}{3}}{3} = \frac{\frac{1}{3}}{3} = \frac{1}{3} : 3 = \frac{1}{3} \cdot \frac{1}{3} = \frac{1}{9}$

d)  $\left(2 - \frac{7}{8}\right) \cdot \frac{8}{9} : \left(\frac{5}{8} + \frac{5}{6}\right) = \frac{8}{8} \cdot \frac{8}{9} : \frac{35}{24} = 1 : \frac{35}{24} = 1 \cdot \frac{24}{35} = \frac{24}{35}$

↳  $\frac{16}{8} - \frac{7}{8} = \frac{9}{8}$      $\frac{5}{8} + \frac{5}{6} = \frac{15+20}{24} = \frac{35}{24}$

Zjednoduš

VZOREC

e)  $(3+a)^2 - (3 \cdot a)^2 - 3^2 = 9 + 6a + a^2 - 9a^2 - 9 = 6a - 8a^2$

$(3+a)(3+a) = 9 + 3a + 3a + a^2$

f)  $2n \cdot (3-n) + 2 \cdot (3n \cdot n) - n \cdot (3 \cdot n) = 6n - 2n^2 + 6n^2 - 3n^2 = 6n + n^2$

Řeš rovnici:

$\frac{2 \cdot 5x}{1 \cdot 3}$

g)  $2 \cdot \frac{5x}{6} - \frac{1}{3} = x - \frac{1}{2}$

$\frac{5x}{3} - \frac{1}{3} = x - \frac{1}{2} \quad / \cdot 6$

$10x - 2 = 6x - 3$

$4x = -1 \quad / : 4$

$x = -\frac{1}{4}$

Řeš rovnici:

h)  $y - \frac{1-3y}{2} = \frac{7}{4} + \frac{5y}{3} \quad / \cdot 12$

NEZIKROK:

$12y - 6 \cdot (1-3y) = 3 \cdot 7 + 4 \cdot 5y$

$12y - 6 + 18y = 21 + 20y$

$-6 + 30y = 21 + 20y$

$30y - 20y = 21 + 6$

$10y = 27 \quad / : 10$

$y = 2,7 \quad y = \frac{27}{10}$

Test z aritmetiky 9

Cermat 2018 PBD (14b)

$$\sqrt{6400 + 3600} = \sqrt{10\,000} = 100$$

a)  $100 + 1 \cdot \sqrt{6400 + 60^2} = 100 + 1 \cdot 100 = 100 + 0,01 = 100,01$

b)  $0,005 \cdot 10^2 - 1,2 : 0,02 = 0,5 - 60 = -59,5$   
 $\hookrightarrow 120 : 2$

c)  $(0,5 + \frac{2}{5}) : (2 - \frac{7}{8}) = (\frac{5}{10} + \frac{4}{10}) : (\frac{16}{8} - \frac{7}{8}) = \frac{9}{10} : \frac{9}{8} = \frac{9}{10} \cdot \frac{8}{9} = \frac{4}{5}$

d)  $\frac{\cancel{8} \cdot \frac{2}{\cancel{8}} - \frac{3}{5} : \frac{6}{15}}{2} = \frac{\frac{2}{3} - \frac{3}{5} \cdot \frac{15}{6}}{2} = \frac{2 \cdot 2 - \frac{3 \cdot 3}{2 \cdot 3}}{2} = \frac{4 - 9}{2} = -\frac{5}{2} = -\frac{5}{6} : 2 = -\frac{5}{6} \cdot \frac{1}{2} = -\frac{5}{12}$   
 NEZAPOMENOUT ZNAMENKO ⊖

Zjednoduš  $(2+3a)^2 - (2-3a)^2 = 4 + 12a + 9a^2 - 4 + 12a - 9a^2 = 24a$   
 VZOREC VZOREC + OTOČN ZNAMENKO

dlka:  $(2+3a)(2+3a) = 4 + 6a + 6a + 9a^2$   
 $dlka: -(2-3a)(2-3a) = -[4 - 6a - 6a + 9a^2]$

f)  $\frac{1}{2} \cdot n \cdot (2-3n) + 3 \cdot (n+2n) - n \cdot (3-n) = n - \frac{3}{2}n^2 + 9n - 3n + n^2 = -\frac{1}{2}n^2 + 7n$   
 $-\frac{3}{2}n^2 + n^2 = -\frac{1}{2}n^2$   
 $-\frac{3}{2} + \frac{2}{2} = -\frac{1}{2}$

Řeš rovnici:

g)  $x \cdot (x+2) + 0,6 = x \cdot x + \frac{1}{5}$

$$x^2 + 2x + 0,6 = x^2 + \frac{1}{5}$$

$$2x + 0,6 = \frac{1}{5}$$

$$2x + 0,6 = 0,2$$

$$2x = 0,2 - 0,6$$

$$2x = -0,4 \quad /:2$$

$$x = -0,2$$

$$10x + 3 = 1$$

$$10x = -2$$

$$x = -\frac{2}{10}$$

$$x = -\frac{1}{5}$$

Řeš rovnici:  $\hookrightarrow \frac{2y}{5}$

h)  $\frac{2y-3}{4} - 2 \cdot \frac{y}{5} = \frac{2-y}{2} - 1 \quad /:20$

$$10y - 15 - 8y = 20 - 10y - 20$$

$$-15 + 2y = -10y$$

$$2y + 10y = 15$$

$$12y = 15 \quad /:3$$

$$4y = 5$$

$$y = \frac{5}{4}$$

$$\begin{array}{r} 128,0 \\ - 2,9 \\ \hline 125,1 \end{array}$$

a)  $25,6 : 0,2 - 10^2 \cdot 0,029 = 128 - 2,9 = 125,1$   
 $\hookrightarrow 256 : 2 = 128$

$$\begin{array}{r} 120,0 \\ - 3,6 \\ \hline 116,4 \end{array}$$

b)  $\frac{\sqrt{1,2^2}}{0,01} - \frac{(\sqrt{0,01})^2}{10} \cdot 3600 = \frac{1,2}{0,01} - \frac{0,01}{10} \cdot 3600 = 120 - 0,001 \cdot 3600 = 120 - 3,6 = 116,4$

$\frac{1,2 \cdot 100}{0,01 \cdot 100} = \frac{120}{1} = 120$      $1,2 : 0,01 = 120 : 1 = 120$      $0,01 : 10 = 0,001$

c)  $\frac{\frac{1}{4} + \frac{2}{3}}{\left(3 - \frac{9}{4}\right) \cdot \frac{8}{3}} = \frac{\frac{3+8}{12}}{\left(\frac{12-9}{4}\right) \cdot \frac{8}{3}} = \frac{\frac{11}{12}}{\frac{2 \cdot 8}{4 \cdot 3}} = \frac{11}{12} : \frac{2}{3} = \frac{11}{12} \cdot \frac{3}{2} = \frac{11}{8}$

d)  $3 : \frac{2 \cdot 6}{2+6} - \frac{12}{3} \cdot \frac{5}{8} = 3 : \frac{12}{8} - \frac{3}{3} \cdot \frac{5}{2} = \frac{3}{1} \cdot \frac{8}{12} - \frac{5}{2} = \frac{8}{4} - \frac{5}{2} = \frac{4}{2} - \frac{5}{2} = -\frac{1}{2}$

Zjednoduř

e)  $a - a^2 + 2 - 2 \cdot (a+1) \cdot (1-a) = a - a^2 + 2 - 2 + 2a^2 = a^2 + a$   
VZOREC + NÁSOBÍM (-2)  
1-a

alt.:  $-2 \cdot (a+1)(1-a) = +(-2a-2)(1-a) = -2a+2a^2-2+2a$   
 alt.:  $-2 \cdot (a+1)(1-a) = -2 \cdot [a - a^2 + 1 - a] = -2 \cdot [-a^2 + 1]$

f)  $\left(n - \frac{5}{2}\right) : 2 + \left(\frac{1}{2} - n\right)^2 = \frac{n}{2} - \frac{5}{4} + \frac{1}{4} - n + n^2 = n^2 - \frac{1}{2}n - \frac{4}{4} = n^2 - \frac{1}{2}n - 1 \xrightarrow{2 \cdot \text{voj}} n^2 - 0,5n - 1$   
VZOREC

$\hookrightarrow$  alt.:  $\left(n - \frac{5}{2}\right) \cdot \frac{1}{2} \quad \left(\frac{1}{2} - n\right) \left(\frac{1}{2} - n\right) = \frac{1}{4} - \frac{1}{2}n - \frac{1}{2}n + n^2 \quad \frac{1}{2}n - \frac{2}{2}n = -n$

Řeř rovníci:

Řeř rovníci:

g)  $0,4 + \frac{4x}{5} - 1 = 0,2x - \frac{3}{2} \quad / \cdot 10$

$4 + 8x - 10 = 2x - 15$

$8x - 6 = 2x - 15$

$8x - 2x = -15 + 6$

$6x = -9 \quad /:3$

$2x = -3 \quad /:2$

$x = -\frac{3}{2} \xrightarrow{2 \cdot \text{voj}} x = -1,5$

h)  $\frac{3y-1}{3} - \frac{5y-2}{6} = \frac{3}{4}y + 2 \quad / \cdot 12$

MEZIKROK  $4 \cdot (3y-1) - 2 \cdot (5y-2) = 9y + 24$

$12y - 4 - 10y + 4 = 9y + 24$

$2y = 9y + 24$

$2y - 9y = 24$

$-7y = 24 \quad /: (-7)$

$y = -\frac{24}{7}$

$$\begin{array}{r} 1,5 \\ 1,5 \\ \hline 2,25 \end{array} \quad \begin{array}{r} 2,25 \\ -0,09 \\ \hline 2,16 \end{array}$$

a)  $1,5^2 - 0,3^2 = 2,25 - 0,09 = 2,16$

$$2100 : 7 = 300$$

b)  $210 : (-0,7) + \sqrt{\frac{8^2+8}{6^2-4}} = -300 + \frac{3}{2}$

$$\left[ \begin{array}{l} \rightarrow -300 + 1,5 = -298,5 \\ \rightarrow -\frac{600}{2} + \frac{3}{2} = -\frac{597}{2} \end{array} \right.$$

$$\sqrt{\frac{64+8}{36-4}} = \sqrt{\frac{72}{32}} = \sqrt{\frac{36}{16}} = \frac{6}{4} = \frac{3}{2}$$

c)  $0,2 - 0,2 \cdot \frac{5}{12} - \left(-\frac{7}{30}\right) = \frac{1 \cdot 12}{5 \cdot 12} - \frac{1 \cdot 5}{5 \cdot 12} + \frac{7 \cdot 2}{30 \cdot 2} = \frac{12}{60} - \frac{5}{60} + \frac{14}{60} = \frac{21}{60} = \frac{7}{20}$

$$\frac{2}{10} = \frac{1}{5}$$

d)  $\frac{\frac{5}{6} : \frac{15}{8} + \frac{4}{9}}{2 \cdot \left(1 - \frac{1}{4}\right) : \frac{1}{24}} = \frac{\frac{5}{6} \cdot \frac{8}{15} + \frac{4}{9}}{2 \cdot \frac{3}{4} : \frac{1}{24}} = \frac{\frac{4}{3} + \frac{4}{9}}{\frac{3}{2} \cdot \frac{24}{1}} = \frac{\frac{8}{3}}{\frac{36}{1}} = \frac{8}{3} : \frac{36}{1} = \frac{8}{3} \cdot \frac{1}{36} = \frac{2}{81}$

Zjednoduř  $-3 \cdot \left(\frac{2a}{3} + a^2\right)$

e)  $2a \left(2 - \frac{a}{2}\right) - \left(\frac{2a}{3} + a^2\right) \cdot 3 = 4a - a^2 - 2a - 3a^2 = 2a - 4a^2$

$$\frac{2a \cdot \frac{a}{2} - 3 \cdot \frac{2a}{3}}{1-2n+n^2} \quad \text{ROZDĚL X2}$$

f)  $2 \cdot (1-n)^2 + (n+2)^2 - 3 \cdot (2+n \cdot \frac{n}{n^2}) = 2 - 4n + 2n^2 + n^2 + 4n + 4 - 6 - 3n^2 = 0$

alte:  $2 \cdot (1-n)(1-n) = (2-2n)(1-n)$

Řeř rovníci:

g)  $\frac{x-2}{0,2} + 0,6 = x + \frac{1}{5}$

$$\frac{(x-2) \cdot 5}{0,2 \cdot 5} = \frac{5x-10}{1} = 5x-10$$

$$5x - 10 + 0,6 = x + \frac{1}{5} \quad /:5$$

$$25x - 50 + 3 = 5x + 1$$

$$25x - 47 = 5x + 1$$

$$25x - 5x = 1 + 47$$

$$20x = 48 \quad /:2$$

$$10x = 24 \quad /:2$$

$$5x = 12 \quad /:5$$

$$x = 2,4$$

$$x = \frac{12}{5}$$

Řeř rovníci:

h)  $\frac{y-2-2y}{3} + 3 \cdot \frac{2y}{5} = 2y - \frac{3y-1}{3}$

$$\frac{-2-y}{3} + \frac{6y}{5} = 2y - \frac{3y-1}{3} \quad /:15$$

MEZIVÝPOČ:  $5 \cdot (-2-y) + 18y = 30y - 5 \cdot (3y-1)$

$$-10 - 5y + 18y = 30y - 15y + 5$$

$$-10 + 13y = 15y + 5$$

$$13y - 15y = 5 + 10$$

$$-2y = 15 \quad /: (-2)$$

$$y = -\frac{15}{2} \rightarrow y = -7,5$$

# Test z aritmetiky 12

Cermat 2019 PAD (12b)

$$a) (6-4) \cdot \frac{11}{8} + \frac{9}{14} \cdot \frac{7}{8} = 2 \cdot \frac{11}{8} + \frac{3}{4} = \frac{11}{4} + \frac{3}{4} = \frac{14}{4} = \frac{7}{2}$$

$$b) \frac{\frac{2 \cdot 3}{6} - \frac{4}{2 \cdot 3}}{\frac{2+3}{6}} = \frac{\frac{6}{6} - \frac{4}{6}}{\frac{5}{6}} = \frac{\frac{2}{6}}{\frac{5}{6}} = \frac{2}{6} : \frac{5}{6} = \frac{2}{6} \cdot \frac{6}{5} = \frac{2}{5}$$

Zjednoduř

$$c) (3a-2) \cdot (-2a) = -6a^2 + 4a$$

$$d) (3x-4)^2 = \underline{9x^2 - 24x + 16}$$

↪ (3x-4)(3x-4) = 9x<sup>2</sup> - 12x - 12x + 16

$$e) (2+n) \cdot (3n-3) + (3n-n) \cdot 2 - n \cdot (3-5) = \underline{6n - 6} + \underline{3n^2 - 3n} + \underline{4n + 2n} = 3n^2 - 6 + 3n^2$$

Řeř rovnici:

$$f) 0,6x - \frac{1}{2} = 1,4x + 1,5 \quad / \cdot 10$$

$$\begin{aligned} 6x - 5 &= 14x + 15 \\ 6x - 14x &= 15 + 5 \\ -8x &= 20 \quad /:4 \\ -2x &= 5 \quad /:(-2) \\ x &= -\frac{5}{2} \quad \xrightarrow{2 \cdot n} x = -2,5 \end{aligned}$$

Řeř rovnici:

$$g) \frac{3-2y}{3} = \frac{1-2y}{4} + \frac{y+3}{6} \quad / \cdot 12$$

$$\begin{aligned} 12-8y &= 3-6y+2y+6 \\ 12-8y &= 9-4y \\ -8y+4y &= 9-12 \\ -4y &= -3 \quad /:(-1) \\ 4y &= 3 \quad /:4 \\ y &= \frac{3}{4} \quad \xrightarrow{2 \cdot n} y = 0,75 \end{aligned}$$

Test z aritmetiky 13  
Cermat 2019 PBD (14b)

a)  $\sqrt{10^2 \cdot 0,0025} = \begin{cases} \sqrt{100 \cdot 0,0025} = \sqrt{0,25} = 0,5 \\ 10 \cdot 0,05 = 0,5 \end{cases}$

b)  $5 : 0,2 - (-0,3 + 0,5) = 25 - (0,2) = 25 - 0,2 = 24,8$   
 $50 : 2$   $\frac{25,0}{-0,2} = 24,8$

c)  $\frac{1 - \frac{1}{3}}{-6^2} = \frac{\frac{3}{3} - \frac{1}{3}}{-36} = \frac{\frac{2}{3}}{-36} = -\frac{2}{36} = -\frac{2}{3} : 36 = -\frac{2}{3} \cdot \frac{1}{36} = -\frac{1}{54}$

d)  $12 \cdot \left(\frac{2}{3} - \frac{1}{2}\right) - \frac{5}{2} + \frac{2}{3} = 12 \cdot \left(\frac{4-3}{6}\right) - \frac{5}{2} + \frac{2}{3} = 12 \cdot \frac{1}{6} - \frac{5}{2} + \frac{2}{3} = 2 - \frac{5}{2} + \frac{2}{3} = \frac{12}{6} - \frac{15}{6} + \frac{4}{6} = \frac{1}{6}$

Zjednoduš VZOREC

e)  $(2a+3b)^2 = 4a^2 + 12ab + 9b^2$   
 $\hookrightarrow (2a+3b)(2a+3b) = 5$

f)  $3e \cdot (2-f) - 2f \cdot (e-3f) = 6e - 3ef - 2ef + 6f^2 = 6e - 5ef + 6f^2$

g)  $(1+3n)(1+3n) + (1+3n) \cdot (1-3n) - 2 = 1 + 6n + 9n^2 + 1 - 3n^2 - 2 = 6n$   
 $1 + 3n + 3n + 9n^2 + 1 - 3n + 3n - 9n^2 - 2$

Řeš rovnici:

h)  $2 \cdot (3 - 0,75x) + x = 7 - \frac{x}{2}$   
 $6 - 1,5x + x = 7 - \frac{x}{2} \quad / \cdot 2$   
 $12 - 3x + 2x = 14 - x$   
 $12 - x = 14 - x$   
 $-x + x = 14 - 12$   
 $0 = 2$   
 ROVNICE NEMÁ ŘEŠENÍ

Řeš rovnici:

i)  $\frac{5}{6} \cdot (y-2) - \frac{2}{3} \cdot y = \frac{y}{2} - \frac{5}{4}$   
 $\frac{5}{6}y - \frac{5}{3} - \frac{2}{3}y = \frac{y}{2} - \frac{5}{4} \quad / \cdot 12$   
 $10y - 20 - 8y = 6y - 15 \quad \leftarrow 12 \cdot \frac{5}{6} \cdot (y-2)$   
 $2y - 20 = 6y - 15$   
 $2y - 6y = -15 + 20$   
 $-4y = 5$   
 $y = -\frac{5}{4} \quad y = -1,25$

Test z aritmetiky 14  
Cermat 2019 PCD (12b)

$$a) \frac{6}{5} - \frac{6}{5} : \frac{9}{10} + 0,3 = \frac{6}{5} - \frac{6}{5} \cdot \frac{10}{9} + \frac{3}{10} = \frac{6 \cdot 6}{6 \cdot 5} - \frac{20 \cdot 2}{15 \cdot 2} + \frac{3 \cdot 3}{10 \cdot 3} = \frac{36 - 40 + 9}{30} = \frac{5}{30} = \frac{1}{6}$$

$$b) \frac{2 + \frac{14}{3}}{2 \cdot \frac{14}{3}} = \frac{\frac{6}{3} + \frac{14}{3}}{\frac{28}{3}} = \frac{\frac{20}{3}}{\frac{28}{3}} = \frac{20}{3} : \frac{28}{3} = \frac{20}{3} \cdot \frac{3}{28} = \frac{5}{7}$$

Zjednoduř

$$c) (5n-2) \cdot (-4n) = -20n^2 + 8n$$

$$d) \left(2x - \frac{1}{2}\right)^2 = 4x^2 - 2x + \frac{1}{4} \quad \left(2x - \frac{1}{2}\right) \left(2x - \frac{1}{2}\right)$$

ROZNAřOBIT

$$e) a \cdot 2a - 2 \cdot (3a-1) \cdot a - a \cdot (7-4) = 2a^2 - 6a^2 + 2a - 3a = -4a^2 - a$$

Řeř rovnici:

$$f) 0,2x + \frac{1}{2} = 2 \cdot (x + 0,25)$$

$$0,2x + \frac{1}{2} = 2x + 0,5 \quad / \cdot 10$$

$$2x + 5 = 20x + 5$$

$$2x - 20x = 5 - 5$$

$$-18x = 0 \quad / : (-18)$$

$$\underline{\underline{x = 0}}$$

Řeř rovnici:

$$g) \frac{9-3y}{6} - \frac{3-2y}{2} = \frac{3-y}{3} \quad / \cdot 6$$

$$\text{NEZIVIFPOČET: } 9-3y - 3 \cdot (3-2y) = 6-2y$$

$$9-3y - 9 + 6y = 6-2y$$

$$3y = 6-2y$$

$$3y + 2y = 6$$

$$5y = 6 \quad / : 5$$

$$y = \frac{6}{5}$$

$$\rightarrow \sqrt{144 \cdot 100} = 12 \cdot 10$$

a)  $\sqrt{14,4 : 0,001} = \sqrt{14400 : 1} = \sqrt{14400} = 120$

$$\begin{array}{r} 2,1 \\ \cdot 0,2 \\ \hline 0,42 \end{array}$$

b)  $0,5 - (-0,3 + 0,5) \cdot 2,1 = 0,5 - 0,2 \cdot 2,1 = 0,5 - 0,42 = 0,08$

c)  $\frac{5 - \frac{2}{5}}{(-7)^2} = \frac{\frac{25}{10} - \frac{4}{10}}{49} = \frac{\frac{21}{10}}{49} = \frac{21}{10} : 49 = \frac{21}{10} \cdot \frac{1}{49} = \frac{3}{70}$

d)  $\frac{5}{3} \cdot \frac{9}{50} \left(1 - \frac{4}{9}\right) - \frac{2}{3} = \frac{5}{3} \cdot \frac{9}{50} \cdot \frac{5}{8} - \frac{2}{3} = \frac{1 \cdot 1 \cdot 5}{3 \cdot 10 \cdot 1} - \frac{2 \cdot 2}{3 \cdot 2} = \frac{1}{6} - \frac{4}{6} = -\frac{3}{6} = -\frac{1}{2}$

Zjednoduř VZOREC  $2 \cdot \frac{x}{2} \cdot \frac{2}{2}$

e)  $\left(\frac{x}{3} + \frac{3}{2}\right)^2 = \frac{x^2}{9} + x + \frac{9}{4}$   
 $\hookrightarrow \left(\frac{x}{3} + \frac{3}{2}\right) \cdot \left(\frac{x}{3} + \frac{3}{2}\right) = \frac{x^2}{9} + \frac{\frac{x}{2} \cdot \frac{3}{2} + \frac{3}{2} \cdot \frac{x}{2}}{\frac{x}{2} + \frac{x}{2} = x} + \frac{9}{4}$

f)  $5a \cdot (0,4b - 2a + 3) = 2ab - 10a^2 + 15a$

g)  $(4+n) \cdot (4-n) + (3n-2) \cdot (-3) = 16 - n^2 - 9n + 6 = -n^2 - 9n + 22$   
 $(4+n)(4-n) = 16 - 4n + 4n - n^2$

Řeř rovnici:

h)  $6x - 2 = 4 \cdot \left(x - \frac{1}{2}\right) + 2x$

$$6x - 2 = 4x - 2 + 2x$$

$$6x - 2 = 6x - 2$$

$$6x - 6x = -2 + 2$$

$$0 = 0$$

NEKONEČNĚ MNOHO  
ŘEŘENÍ

Řeř rovnici: jednu čísl!

i)  $3 - y = \frac{3}{4} \cdot (2y - 1) - 2$   $\cdot 4 \rightarrow 3 - y = \frac{6y}{4} - \frac{3}{4} - 2$   $\cdot 4$

$$12 - 4y = 3 \cdot (2y - 1) - 8$$

$$12 - 4y = 6y - 3 - 8$$

$$12 - 4y = 6y - 11$$

$$-4y - 6y = -11 - 12$$

$$-10y = -23 \quad / \cdot (-1)$$

$$10y = 23$$

$$y = 2,3 \quad y = \frac{23}{10}$$

a)  $(-0,4)^2 + 0,3^2 = 0,16 + 0,09 = 0,25$

b)  $\left(\frac{1}{4} + \frac{5}{6}\right) \cdot \left(\frac{5}{13} - \frac{1}{2}\right) = \left(\frac{3+10}{12}\right) \cdot \left(\frac{10-13}{26}\right) = \frac{13}{12} \cdot \frac{(-3)}{26} = -\frac{1}{8}$

c)  $\frac{\frac{6}{5}}{\frac{7}{6} \cdot 4 - 4 \cdot \frac{5}{12}} = \frac{\frac{6}{5}}{\frac{14}{3} - \frac{5}{3}} = \frac{\frac{6}{5}}{\frac{9}{3}} = \frac{6}{5} : \frac{3}{1} = \frac{6}{5} \cdot \frac{1}{3} = \frac{2}{5}$

Rozlož na součin

d)  $p^2 - 16 = (p-4)(p+4)$  *VZOREC (A+B)(A-B)*

Zjednoduš

e)  $(2x+5)^2 = 4x^2 + 20x + 25$  *VZOREC*

$\hookrightarrow (2x+5)(2x+5)$

f)  $(2n+6) \cdot (4n-5) + (3-5) \cdot 2n - 5n \cdot (n-2n) = 8n^2 - 10n + 24n - 30 - 4n + 5n^2 = 13n^2 + 10n - 30$

Řeš rovnici:

g)  $3,2 - 0,5x - 1 = 0,6 - 1,3x$   $/:10$   
 $32 - 5x - 10 = 6 - 13x$   
 $-5x + 22 = 6 - 13x$   
 $-5x + 13x = 6 - 22$   
 $8x = -16$   $/:8$   
 $x = -2$

Řeš rovnici:

h)  $\frac{5y+3}{8} - \frac{y}{2} = \frac{4-y}{5} + \frac{2y-1}{10}$   $/:40$   
 $5 \cdot (5y+3) - 20y = 8 \cdot (4-y) + 4 \cdot (2y-1)$   
 $25y + 15 - 20y = 32 - 8y + 8y - 4$   
 $5y + 15 = 28$   
 $5y = 28 - 15$   
 $5y = 13$   $/:5$   
 $y = \frac{13}{5}$

$$a) \frac{1}{2} + \frac{8}{5} \cdot \left( \frac{3}{8} - \frac{1}{6} \right) = \frac{1}{2} + \frac{8}{5} \cdot \left( \frac{3-4}{24} \right) = \frac{1}{2} + \frac{8}{5} \cdot \frac{1}{24} = \frac{1}{2} + \frac{1}{3} = \frac{3+2}{6} = \frac{5}{6}$$

$$\frac{1}{2} = \frac{16}{32}$$

$$b) \frac{\frac{7}{4} - 4}{7 - \frac{4}{7}} = \frac{\frac{7}{4} - \frac{16}{4}}{\frac{49}{7} - \frac{4}{7}} = \frac{-\frac{9}{4}}{\frac{45}{7}} = -\frac{9}{4} \cdot \frac{7}{45} = -\frac{9}{4} \cdot \frac{7}{5 \cdot 3} = -\frac{7}{20}$$

$$\frac{7}{1} = \frac{49}{7}$$

Rozlož na součin

$$c) (4a)^2 - 9 \cdot 9 = 16a^2 - 81 = (4a - 9)(4a + 9)$$

Zjednoduš

$$d) \left( \frac{3y}{2} + 2 \right)^2 = \frac{9y^2}{4} + 6y + 4$$

$$\text{ale: } \left( \frac{3y}{2} + 2 \right) \left( \frac{3y}{2} + 2 \right) = \frac{9y^2}{4} + 3y + 3y + 4 = \frac{9y^2}{4} + 6y + 4$$

Zjednodušte a rozložte na součin

$$e) (3n+7) \cdot (-4n+3n) + n \cdot (4n+9) = -3n^2 - 7n + 4n^2 + 9n = n^2 + 2n = n \cdot (n+2)$$

Řeš rovnici:

$$f) 2,5 \cdot (2x - 0,4) + x = 2,5x + 0,4 \quad / \cdot 10$$

$$25 \cdot (2x - 0,4) + 10x = 25x + 4$$

$$50x - 10 + 10x = 25x + 4$$

$$60x - 10 = 25x + 4$$

$$60x - 25x = 4 + 10$$

$$35x = 14 \quad / : 7$$

$$5x = 2 \quad / : 5$$

$$\text{ale: } x = 0,4$$

$$x = \frac{2}{5}$$

Řeš rovnici:

$$g) y - \frac{2-5y}{10} = \frac{5y-8}{15} - 2 \quad / \cdot 30$$

$$\text{mezivýpočet: } 30y - 3 \cdot (2-5y) = 2 \cdot (5y-8) - 60$$

$$30y - 6 + 15y = 10y - 16 - 60$$

$$-6 + 45y = 10y - 76$$

$$45y - 10y = -76 + 6$$

$$35y = -70 \quad / : 35$$

$$y = -2$$

# Test z aritmetiky 18

Cermat 2021 PAD (12b)

$$a) \left( \frac{5 \cdot 10^5 + 4}{8 \cdot 9 \cdot 4 \cdot 9} \right) : \left( \frac{8 \cdot 1}{8 \cdot 6} \right) = \left( \frac{25}{36} - \frac{16}{36} \right) : \left( \frac{4}{3} \right) = \frac{9}{36} \cdot \frac{3}{4} = \frac{3}{16}$$

$$b) \frac{2 - \frac{13}{10}}{\frac{5}{3} - \frac{1}{2}} = \frac{\frac{20}{10} - \frac{13}{10}}{\frac{10-3}{6}} = \frac{\frac{7}{10}}{\frac{7}{6}} = \frac{7}{10} : \frac{7}{6} = \frac{7}{10} \cdot \frac{6}{7} = \frac{3}{5}$$

Rozlož na součin podle vzorce

$$c) 9a^2 - 30a + 25 = (3a - 5)^2$$

$(A - B)^2$

Zjednodušte

$$d) (3x+y) \cdot (3x-2) = 3x^2 - 6x + 3xy - 2y$$

VZOREC

$$e) (4n-1) \cdot (4n+1) - 8n \cdot (n-1) = 16n^2 - 1 - 8n^2 + 8n = 8n^2 + 8n - 1$$

$$\hookrightarrow (4n-1)(4n+1) = 16n^2 + 4n - 4n + 1$$

Řeš rovnici:

$$f) 0,3 \cdot 2 - 0,5 \cdot 2 + 0,4x = x + 3,8$$

$$0,6 - x + 0,4x = x + 3,8 \quad / \cdot 10$$

$$6 - 10x + 4x = 10x + 38$$

$$6 - 6x = 10x + 38$$

$$-6x - 10x = 38 - 6$$

$$-16x = 32 \quad / : (-16)$$

$$\underline{\underline{x = -2}}$$

Řeš rovnici:

$$g) \frac{3}{4} \cdot (4-y) + \frac{3}{2} \cdot (y+2) = 6 + \frac{3y}{2}$$

$$3 \cdot (4-y) + 6 \cdot (y+2) = 24 + 6y \quad / \cdot 4$$

$$12 - 3y + 6y + 12 = 24 + 6y$$

$$24 + 3y = 24 + 6y$$

$$3y - 6y = 24 - 24$$

$$-3y = 0 \quad / : (-3)$$

$$\underline{\underline{y = 0}}$$

Test z aritmetiky 19

Cermat 2021 PBD (13b)

a)  $\sqrt{\frac{16}{0,1} + 9} = \sqrt{160 + 9} = \sqrt{169} = 13$

$\hookrightarrow 16 : 0,1 = 160 : 1 = 160$

b)  $\frac{2 - \frac{4}{7}}{3 - \frac{13}{21}} = \frac{\frac{14}{7} - \frac{4}{7}}{\frac{63}{21} - \frac{13}{21}} = \frac{\frac{10}{7}}{\frac{50}{21}} = \frac{1}{7} \cdot \frac{21}{50} = \frac{3}{5}$

$\frac{3}{1} = \frac{63}{21}$

$\hookrightarrow -\frac{1}{40} \cdot \frac{8}{1}$

c)  $\left(\frac{3}{8} - \frac{2}{5}\right) \cdot 5 - \frac{3}{4} = \left(\frac{15}{40} - \frac{16}{40}\right) \cdot 5 - \frac{3}{4} = \frac{-1}{40} \cdot 5 - \frac{3 \cdot 2}{4 \cdot 2} = -\frac{1}{8} - \frac{6}{8} = -\frac{7}{8}$

Zjednoduř

d)  $(2-x) \cdot 3x - 2x = 6x - 3x^2 - 2x = 4x - 3x^2$

$-\frac{1}{2}y - \frac{1}{2}y = -\frac{2}{2}y = -y$

$(a-b)^2$

e)  $\left(y - \frac{1}{2}\right)^2 = y^2 - y + \frac{1}{4}$

ale:  $\left(y - \frac{1}{2}\right)\left(y - \frac{1}{2}\right) = y^2 - \frac{1}{2}y - \frac{1}{2}y + \frac{1}{4} = y^2 - y + \frac{1}{4}$

Zjednoduř a rozlož na součin

f)  $5^2 - (a^2 + 16) = 25 - a^2 - 16 = 9 - a^2 = (3-a)(3+a)$

Řeř rovnici:

g)  $2x \cdot (3,2 - 2,3) = 2x - (3,2 - 2,3)$

$1,8x = 2x - 0,9 \quad / \cdot 10$

$18x = 20x - 9$

$18x - 20x = -9$

$-2x = -9 \quad / \cdot (-1)$

$2x = 9 \quad / : 2$

$x = \frac{9}{2}$  nebo  $x = 4,5$

Řeř rovnici:

h)  $\frac{y+3}{3} + \frac{3}{8} \cdot (y+1) = \frac{2y-1}{4} + 1$

$\frac{y+3}{3} + \frac{3y}{8} + \frac{3}{8} = \frac{2y-1}{4} + 1 \quad / \cdot 24$

$8y + 24 + 9y + 9 = 12y - 6 + 24$

$17y + 33 = 12y + 18$

$17y - 12y = 18 - 33$

$5y = -15 \quad / : 5$

$y = -3$

$$a) \left(\frac{3}{4} + \frac{13}{6}\right) \cdot \left(\frac{2}{5} - 1\right) = \left(\frac{9}{12} + \frac{26}{12}\right) \cdot \left(\frac{2}{5} - \frac{5}{5}\right) = \frac{35}{12} \cdot \frac{(-3)}{5} = -\frac{7}{4}$$

$$b) \frac{3 \cdot 2 - 4 \cdot \frac{2}{7}}{2} = \frac{\frac{6}{7} - \frac{8}{7}}{2} = \frac{\frac{42}{35} - \frac{40}{35}}{2} = \frac{\frac{2}{35}}{2} = \frac{2}{35} : 2 = \frac{2}{35} \cdot \frac{1}{2} = \frac{1}{35}$$

Rozlož na součin podle vzorce

$$A^2 - B^2$$

$$c) (4 \cdot a)^2 - 81 = (4a - 9)(4a + 9)$$

Zjednodušte

$$d) 2 \cdot (3y - x) \cdot (5 - y) = (6y - 2x)(5 - y) = 30y - 6y^2 - 10x + 2xy$$

$$2 \cdot (3y - x)(5 - y) = 2 \cdot [15 - 3y^2 - 5x + xy]$$

$$e) (4n+1)^2 + 3 \cdot (n-1) - (3n+n) \cdot 2n = 16n^2 + 8n + 1 + 3n - 3 - 8n^2 = 8n^2 + 11n - 2$$

VZOREC

$$\text{alte: } (4n+1)(4n+1) = 16n^2 + 4n + 4n + 1$$

Řeš rovnici:

$$\frac{0,4}{0,04} \cdot \frac{0,1}{0,04} = 0,32 : 0,1 = 3,2$$

$$f) 0,4 \cdot 0,1x + 0,32 : 0,1 = 0,2x$$

$$0,04x + 3,2 = 0,2x \quad / \cdot 100$$

$$4x + 320 = 20x$$

$$320 = 20x - 4x$$

$$320 = 16x \quad / : 16$$

$$\underline{x = 20}$$

Řeš rovnici:

$$g) \frac{y-4}{5} - \frac{y}{10} = \frac{3+y}{2} - 2 \quad / \cdot 10$$

$$2y - 8 - y = 15 + 5y - 20$$

$$y - 8 = 5y - 5$$

$$y - 5y = -5 + 8$$

$$-4y = 3 \quad / : (-4)$$

$$y = -\frac{3}{4}$$

$$y = -0,75$$

a)  $\frac{0,25}{0,025} : 0,2 = \frac{10 : 0,2}{1} = 100 : 2 = 50$

$\hookrightarrow 0,25 : 0,025 = 250 : 25 = 10$

b)  $\left(\frac{5}{8} - \frac{5}{12}\right) \cdot 4 - 2 \cdot \left(\frac{3}{4} - \frac{2}{3}\right) = \left(\frac{15}{24} - \frac{10}{24}\right) \cdot 4 - 2 \cdot \left(\frac{3}{12} - \frac{8}{12}\right) = \frac{5}{24} \cdot 4 - 2 \cdot \frac{1}{12} = \frac{5}{6} - \frac{1}{6} = \frac{4}{6} = \frac{2}{3}$

c)  $\frac{\left(\frac{27}{10} \cdot \frac{5}{9} - 4\right) : 3}{5} = \frac{\left(\frac{3}{2} - \frac{8}{2}\right) : \frac{3}{1}}{5} = \frac{-\frac{5}{2} \cdot \frac{1}{3}}{5} = \frac{-\frac{5}{6}}{5} = -\frac{5}{6} : 5 = -\frac{5}{6} \cdot \frac{1}{5} = -\frac{1}{6}$

Z daného výrazu vytkněte  $(-3x)$ .

d)  $-6x^2 - 3x + 9xy = (-3x) \cdot (2x + 1 - 3y)$

$\hookrightarrow$  NEVÍM SI JISTÝ? ZK: ROZVÁSOBÍME

Zjednoduš a rozlož na součin

e)  $(5-y)(5+y) + 3 \cdot (y^2 - 10) - (2y-3) \cdot y = 25 - y^2 + 3y^2 - 30 - 2y^2 + 3y = 3y - 5$

$\hookrightarrow (5-y)(5+y) = 25 + 5y - 5y - y^2$

Doplňte čísla tak, aby platila rovnost.

e)  $(7a - 4b)^2 = 49a^2 - 56ab + 16b^2$   $B = 4b$

$2AB = 56ab = 2 \cdot 7a \cdot 4b$

$56ab : 2 = 28ab$

$28ab : 4b = 7a$

Řeš rovnici:

g)  $2,5 \cdot (2 - 3x) = \frac{5x + 10}{2}$

$5 - 7,5x = \frac{5x + 10}{2}$   $\cdot 2$

$10 - 15x = 5x + 10$

$-15x - 5x = 10 - 10$

$-20x = 0$   $\cdot (-20)$

$x = 0$

Řeš rovnici:

h)  $\frac{5}{3} \cdot (y-1) + \frac{5}{6} \cdot (11-2y) - \frac{3}{4} \cdot y = 0$   $\cdot 12$

$\frac{5}{3}y - \frac{5}{3} + \frac{55}{6} - \frac{10y}{6} - \frac{3}{4}y = 0$   $\cdot 12$

$20y - 20 + 110 - 20y - 9y = 0$

$90 - 9y = 0$

$-9y = -90$   $\cdot (-9)$

$y = 10$

a)  $\frac{7^2 - \sqrt{7^2}}{\sqrt{49}} = \frac{49 - 7}{7} = \frac{42}{7} = 6$

b)  $\frac{8}{5} \cdot \left( \frac{5}{6} \cdot \frac{7}{10} - \frac{2 \cdot 5}{2 \cdot 6} \right) = \frac{8}{5} \cdot \left( \frac{7}{12} - \frac{10}{12} \right) = \frac{8}{5} \cdot \left( -\frac{3}{12} \right) = -\frac{8}{5} \cdot \frac{1}{4} = -\frac{2}{5}$

$\rightarrow \frac{12 - 10}{15}$

c)  $\frac{\left( \frac{4}{5} - \frac{2}{3} \right) \cdot \frac{5}{8}}{\frac{2}{3}} = \frac{\frac{2}{3} \cdot \frac{5}{8}}{\frac{2}{3}} = \frac{1}{12} \cdot \frac{3}{2} = \frac{1}{8}$

Z daného výrazu vytkněte 3y.

d)  $3y^2 - 9y + 6xy = 3y \cdot (y - 3 + 2x)$

$3y^2 : 3y = y$     $-9y : 3y = -3$     $6xy : 3y = 2x$

Zjednoduř a rozlož na součin

f)  $(4+3n) \cdot (3n-2n) = (n-1) \cdot 5n = 4n + 3n^2 - 5n^2 + 5n = -2n^2 + 9n = n \cdot (-2n + 9)$

$(4+3n) \cdot n - 5n \cdot (n-1)$

Zjednoduř

*ROZDIL  $(n+B)^2$*

e)  $\left( x + \frac{3}{2} \right)^2 = x^2 + 3x + \frac{9}{4}$

*rozřn.*  
 $\left( x + \frac{3}{2} \right) \cdot \left( x + \frac{3}{2} \right) = x^2 + \frac{3}{2}x + \frac{3}{2}x + \frac{9}{4} = x^2 + \frac{6}{2}x + \frac{9}{4} = x^2 + 3x + \frac{9}{4}$

Řeř rovnici:

g)  $5 \cdot 0,4 - 3x : 2 = 0,5x + 7$

$2 - 1,5x = 0,5x + 7$   
 $-1,5x - 0,5x = 7 - 2$   
 $-2x = 5 \quad /: (-2)$   
 $x = -\frac{5}{2} \quad x = -2,5$

Řeř rovnici:

h)  $\frac{3-y}{3} + \frac{3}{5} \cdot (y+1) + \frac{y}{3} = y$

$\frac{3-y}{3} + \frac{3}{5}y + \frac{3}{5} + \frac{y}{3} = y \quad / \cdot 15$

$15 - 5y + 9y + 3 + 5y = 15y$

$9y + 24 = 15y$

$9y - 15y = -24$

$-6y = -24 \quad /: (-6)$

$y = 4$

*z hlavy:*

$\frac{3}{15} \cdot \frac{3}{5} \cdot (y+1)$

$9 \cdot (y+1)$

Test z aritmetiky 23

Cermat 2022 PBD (13b)

a)  $(-6)^2 - 3 \cdot (-3) = 36 + 9 = 45$   
 $(-6)(-6)$

b)  $\frac{7}{5} \cdot \frac{3}{8} \cdot \frac{10}{21} + \frac{3}{10} = \frac{7}{\cancel{5}^1} \cdot \frac{3}{\cancel{8}^2} \cdot \frac{\cancel{10}^1}{\cancel{21}^3} + \frac{3}{10} = \frac{1}{4} + \frac{3}{10} = \frac{5}{20} + \frac{6}{20} = \frac{11}{20}$

c)  $\frac{2 \cdot 1}{2 \cdot 4} - \frac{5}{8} = \frac{\frac{2}{\cancel{2}^1} - \frac{5}{8}}{\frac{4}{\cancel{2}^1}} = \frac{-\frac{3}{8}}{\frac{4}{\cancel{2}^1}} = -\frac{3}{8} : \frac{4}{\cancel{2}^1} = -\frac{3}{8} \cdot \frac{\cancel{4}^1}{2} = -\frac{3}{10}$   
 $\frac{3}{1} \cdot \frac{5}{12}$

Uprav a rozlož na součin

d)  $x \cdot x - x + 2x^2 = x^2 - x + 2x^2 = 3x^2 - x = x \cdot (3x - 1)$   
 UPRAVENO

Zjednoduš  
 $(A - B)^2 \rightarrow$  **VZOREC**

e)  $(5b - 0,4a)^2 = 25b^2 - 4ab + 0,16a^2$

roz.  $(5b - 0,4a)(5b - 0,4a) = 25b^2 - 2ab - 2ab + 0,16a^2 = 25b^2 - 4ab + 0,16a^2$

f)  $(2n-3) \cdot (4n-2) + (n-3) \cdot (n+3) = 8n^2 - 4n - 12n + 6 + n^2 - 9 = 9n^2 - 16n - 3$   
 $\hookrightarrow$  roz:  $n^2 - 3n + 3n - 9$

Řeš rovnici:

g)  $5 \cdot (0,2x + 1) = (8 - 6x) : 2$

$x + 5 = 4 - 3x$

$x + 3x = 4 - 5$

$4x = -1 \quad /:4$

$x = -\frac{1}{4} \quad x = -0,25$

Řeš rovnici:

h)  $\frac{y-5}{2} + \frac{3-y}{6} = 1 - \frac{2y}{3} \quad / \cdot 6$

$3y - 15 + 3 - y = 6 - 4y$

$2y - 12 = 6 - 4y$

$2y + 4y = 6 + 12$

$6y = 18 \quad /:6$

$y = 3$

Test z aritmetiky 24

Cermat 2022 PCD (13b)

a)  $\frac{10^2 \cdot (10^2 - 1)}{10 \cdot 10^2 + 10^2} = \frac{100 \cdot (100 - 1)}{10 \cdot 100 + 100} = \frac{100 \cdot 99}{1000 + 100} = \frac{100 \cdot 99}{1100} = \frac{99}{11} = 9$

b)  $\frac{1}{3} \cdot \left(5 - \frac{13}{5}\right) : 20 = \frac{1}{3} \cdot \frac{12}{5} : 20 = \frac{1}{5} \cdot \frac{1}{20} = \frac{1}{25}$   
 $L: \frac{25 - 13}{5}$

c)  $\frac{\frac{2}{3} - \frac{3}{2}}{\frac{2}{3} : \frac{3}{2}} = \frac{\frac{4-9}{6}}{\frac{2}{3} \cdot \frac{2}{3}} = \frac{-\frac{5}{6}}{\frac{4}{9}} = -\frac{5}{6} : \frac{4}{9} = -\frac{5}{6} \cdot \frac{9}{4} = -\frac{15}{8}$

! NEKRÁTIT V O! (Warning: Do not cancel across the fraction bar!)

Uprav a rozlož na součin

d)  $(4+x) \cdot x + 2x^2 = 4x + x^2 + 2x^2 = 4x + 3x^2 = x \cdot (4 + 3x)$   
 (Note: Uprav - simplify)

Zjednoduš

e)  $(y-3y) \cdot (y+3y) = -2y \cdot 4y = -8y^2$

f)  $(-n-1)^2 + (1+4n) \cdot (1+4n) = n^2 + 2n + 1 + 1 + 4n + 4n + 16n^2 = 17n^2 + 10n + 2$   
 $(-n-1)(-n-1) = n^2 + n + n + 1$  (Note: rozloz - expand)

Řeš rovnici:

g)  $3 \cdot (2x-1) + \frac{2}{3} = \frac{2}{3} - (x+3)$   
 $3 \cdot (2x-1) + \frac{2}{3} - \frac{2}{3} = - (x+3)$   
 $6x - 3 = -x - 3$   
 $6x + x = -3 + 3$   
 $7x = 0 \quad /:7$   
 $x = 0$

Řeš rovnici:

h)  $\frac{y+1}{6} - \frac{3y}{2} = 2 + \frac{0,5-y}{3}$  (Note:  $2 \cdot 0,5 = 1$ )  
 $y+1 - 9y = 12 + 1 - 2y$   
 $-8y + 1 = 13 - 2y$   
 $-8y + 2y = 13 - 1$   
 $-6y = 12 \quad /: -6$   
 $y = -2$

$$\begin{array}{r} -1,00 \\ +0,08 \\ \hline -0,92 \end{array}$$

a)  $(-3)^2 - 5^2 - 4 \cdot (-4) = 9 - 25 + 16 = 0$   
 $(-3)(-3)$

b)  $(0,08 - 1) : 0,2 = -0,92 : 0,2 = -9,2 : 2 = -4,6$

c)  $\left(\frac{12}{5} \cdot \frac{3}{20} - \frac{5 \cdot 3}{5 \cdot 20}\right) : \frac{7}{25} = \left(\frac{36}{100} - \frac{15}{100}\right) : \frac{7}{25} = \frac{21}{100} \cdot \frac{25}{7} = \frac{3}{4}$

d)  $\frac{12}{2 + \frac{2}{3}} \cdot \frac{2 \cdot \frac{2}{3}}{18} = \frac{12}{\frac{8}{3}} \cdot \frac{\frac{4}{3}}{18} = \frac{9}{2} \cdot \frac{2}{27} = \frac{1}{3}$   
 $\frac{6}{3} + \frac{2}{3} = \frac{8}{3}$   
 $\frac{12}{\frac{8}{3}} = 12 \cdot \frac{3}{8} = \frac{36}{8} = \frac{9}{2}$   
 $\frac{4}{3} : 18 = \frac{4}{3} \cdot \frac{1}{18} = \frac{4}{54} = \frac{2}{27}$

Doplňte čísla tak, aby platila rovnost.

e)  $(y + 5)^2 = y^2 + 10y + 25$   
 $(A+B)^2 = A^2 + 2AB + B^2$   
 $2 \cdot y \cdot 5$

Zjednoduš

f)  $(10x - 8) - x \cdot \sqrt{100 - 64} = 10x - 8 - 6x = 4x - 8$   
 $\hookrightarrow \sqrt{36} = 6$

g)  $(6n+1) \cdot (1-2n-4n) + (1-2n) \cdot (-4n) = (1+6n)(1-6n) - 4n \cdot (1-2n) = 1 - 36n^2 - 4n + 8n^2 = -28n^2 - 4n + 1$   
 $(6n+1)(1-6n) = 6n - 36n^2 + 1 - 6n$

Řeš rovnici:

h)  $x + 0,2 \cdot (5x + 0,9) = x : 5$   
 $5x + 5x + 0,9 = x$   
 $10x - x = -0,9$   
 $9x = -0,9$   
 $x = -0,1$   
nebo  
 $x = -\frac{1}{10}$   
 $5 \cdot 0,2 \cdot (5x + 0,9)$   
 $x + x + 0,9 = \frac{x}{5} \quad / \cdot 100$   
 $100x + 100x + 90 = 20x$   
 $200x - 20x = -90$   
 $180x = -90 \quad / : 18$   
 $10x = -5$   
 $x = -0,5$

Řeš rovnici:

i)  $7 \cdot \frac{y-3}{6} - \frac{6y+6}{9} = \frac{1}{3} \quad / \cdot 18$   
 $\frac{7 \cdot (y-3)}{6} = \frac{7y-21}{6}$   
 $21y - 63 = 2 \cdot (6y+6) = 6$   
 $21y - 63 - 12y - 12 = 6$   
 $9y - 75 = 6$   
 $9y = 6 + 75$   
 $9y = 81 \quad / : 9$   
 $y = 9$

## Test z aritmetiky 26

Cermat 2023 PAD (12b)

$$a) \frac{5}{9} - \frac{5}{9} : 5 = \frac{5}{9} - \frac{5}{9} \cdot \frac{1}{5} = \frac{5}{9} - \frac{1}{9} = \frac{4}{9}$$

$$b) \frac{4-7}{8} \cdot \frac{16}{21} = \frac{-3}{8} \cdot \frac{16}{21} = -\frac{2}{7}$$

$$c) \frac{\frac{3}{5} : \left(\frac{2}{5} + \frac{1}{2}\right)}{\frac{7}{6} + \frac{7}{10}} = \frac{\frac{3}{5} : \left(\frac{4+5}{10}\right)}{\frac{35+21}{30}} = \frac{\frac{3}{5} : \frac{9}{10}}{\frac{56}{30}} = \frac{\frac{3}{5} \cdot \frac{10}{9}}{\frac{28}{15}} = \frac{2}{3} : \frac{28}{15} = \frac{2}{3} \cdot \frac{15}{28} = \frac{5}{14}$$

Uprav a rozlož na součin

$$d) 2 \cdot (x^2 - x) + x = 2x^2 - 2x + x = 2x^2 - x = x \cdot (2x - 1)$$

Zjednoduš

VZOREC  $(a-b)^2$

$$e) \left(\frac{2}{3}a - 3\right)^2 = \frac{4}{9}a^2 - 4a + 9 \quad \left(\frac{2}{3}a - 3\right)\left(\frac{2}{3}a - 3\right) = \frac{4}{9}a^2 - 2a - 2a + 9 = \frac{4}{9}a^2 - 4a + 9$$

$$f) 3n \cdot (2-n+2n) + (2n+1) \cdot (7-n) = 3n \cdot (2+n) = 6n + 3n^2 + 14n - 2n^2 + 7 - n = n^2 + 13n + 7$$

Řeš rovnici:

$$g) 0,5x + 2 \cdot (x+2,5) = 2,5 \cdot (x+3)$$

$$0,5x + 2x + 5 = 2,5x + 7,5$$

$$2,5x + 5 = 2,5x + 7,5$$

$$2,5x - 2,5x = 7,5 - 5$$

$$0x = 2,5$$

ROVNICE NEMÁ ŘEŠENÍ

Řeš rovnici:

$$h) \frac{y+10}{15} + \frac{2y}{5} = 1 - \frac{5-y}{3} \quad / \cdot 15$$

$$y + 10 + 6y = 15 - 25 + 5y$$

$$7y + 10 = 5y - 10$$

$$7y - 5y = -10 - 10$$

$$2y = -20 \quad / : 2$$

$$y = -10$$

Test z aritmetiky 27

Cermat 2023 PBD (13b)

a)  $\sqrt{(-5)^2} - 3^2 = \sqrt{25} - 9 = 5 - 9 = -4$

b)  $\frac{1}{3} \cdot \frac{1}{2} - \frac{8}{9} = \frac{1}{6} - \frac{8}{9} = \frac{3-16}{18} = -\frac{13}{18}$

c)  $\left(2 - \frac{5}{6}\right) : \frac{5}{3} = \left(\frac{12}{6} - \frac{5}{6}\right) : \frac{5}{3} = \frac{7}{6} \cdot \frac{3}{5} = \frac{7}{10}$

d)  $\frac{\frac{2}{3} + \frac{2}{7}}{\left(\frac{9}{14} + \frac{3}{2}\right) \cdot 2} = \frac{\frac{14+6}{21}}{\left(\frac{9}{14} + \frac{21}{14}\right) \cdot 2} = \frac{\frac{20}{21}}{\frac{30}{14} \cdot 2} = \frac{20}{21} : \frac{30}{7} = \frac{20}{21} \cdot \frac{7}{30} = \frac{2}{9}$

Uprav a rozlož na součin

e)  $x \cdot (y-3) + 3 \cdot (x-2y) = xy - 3x + 3x - 6y = xy - 6y = y \cdot (x-6)$

f) Určete pomocí vzorce nejjednodušší výraz, kterým je třeba vynásobit výraz  $3a - 2^2$ , abychom získali výraz  $9a^2 - 16 = (3a-4)(3a+4)$

$(3a-4) \cdot \text{[ ]} = (3a-4)(3a+4)$  odp:  $3a+4$

g)  $(3n+2)^2 - n \cdot (3n+4) + (2n-n) \cdot n = 9n^2 + 12n + 4 - 3n^2 - 4n + n^2 = 7n^2 + 8n + 4$   
 alt:  $(3n+2)(3n+2) = 9n^2 + 6n + 6n + 4$

Řeš rovnici:

h)  $2 + 0,5 \cdot (x-3) = 0,4 \cdot (1,5x+2)$

$2 + 0,5x - 1,5 = 0,6x + 0,8$   $\cdot 10$   
 $20 + 5x - 15 = 6x + 8$   
 $5x + 5 = 6x + 8$   
 $5x - 6x = 8 - 5$   
 $-x = 3$   $\cdot (-1)$   
 $x = -3$

Řeš rovnici:

i)  $3 \cdot \frac{2y-1}{8} = \frac{3y+2}{8} + \frac{y-1}{4}$

$\frac{2y-1}{2} = \frac{3y+2}{8} + \frac{y-1}{8}$   $\cdot 8$   
 $8y-4 = 3y+2 + y-1$   
 $8y-4 = 4y+1$   
 $8y-4y = 1+4$   
 $4y = 5$   
 $y = \frac{5}{4}$

## Test z aritmetiky 28

Cermat 2023 PCD (14b)

a)  $4 + 6 : 2 - 5 \cdot (-3 + 5) = 4 + 3 - 5 \cdot 2 = 4 + 3 - 10 = 7 - 10 = -3$

b)  $\sqrt{1,3^2 - 1,2^2} = \sqrt{1,69 - 1,44} = \sqrt{0,25} = 0,5$

c)  $3 \cdot \frac{2}{7} - \frac{2}{7} = \frac{6}{7} - \frac{2}{7} = \frac{4}{7}$

d)  $1 - \frac{14}{5} : 2 = 1 - \frac{14}{5} \cdot \frac{1}{2} = \frac{5}{5} - \frac{7}{5} = -\frac{2}{5}$

e)  $\frac{\frac{3}{4} + \frac{4}{3}}{\frac{5}{7} - \frac{14}{3}} = \frac{\frac{3+16}{12}}{\frac{10}{3}} = \frac{\frac{25}{12}}{\frac{10}{3}} = \frac{25}{12} \cdot \frac{3}{10} = \frac{25}{4} \cdot \frac{3}{10} = \frac{5}{8}$

Rozlož na součin podle vzorce

f)  $4 \cdot a^2 - 9 = (2a - 3)(2a + 3)$

Zjednoduř

g)  $(2x - 1) \cdot \frac{1}{2} - x = x - \frac{1}{2} - x = -\frac{1}{2}$

**BOREK (A-B)<sup>2</sup>**

h)  $(4n - 3)^2 - 4n \cdot (4n - 3) = 16n^2 - 24n + 9 - 16n^2 + 12n = -12n + 9$

alter:  $(4n - 3)(4n - 3) = 16n^2 - 12n - 12n + 9$

Řeř rovnici:

$10 \cdot 0,3 \cdot (2x + 1) = 3 \cdot (2x + 1) \quad !$

i)  $0,3 \cdot (2x + 1) = 0,2x - 0,7 \quad / \cdot 10$

$3 \cdot (2x + 1) = 2x - 7$

$6x + 3 = 2x - 7$

$6x - 2x = -7 - 3$

$4x = -10 \quad / : 2$

$2x = -5$

$x = -\frac{5}{2} \quad \text{nebo} \quad x = -2,5$

Řeř rovnici:

j)  $y + \frac{5y}{6} = \frac{2y - 1}{4} + \frac{y + 1}{2} \quad / \cdot 12$

$12y + 10y = 6y - 3 + 6y + 6$

$22y = 12y + 3$

$22y - 12y = 3$

$10y = 3$

$y = \frac{3}{10} \quad \text{nebo} \quad y = 0,3$

Test z aritmetiky 29

Cermat 2023 PDD (12b)

a)  $\frac{\frac{2}{3}-1}{\frac{8}{9}} = \frac{\frac{2}{3}-\frac{3}{3}}{\frac{8}{9}} = \frac{-\frac{1}{3}}{\frac{8}{9}} = -\frac{1}{3} \cdot \frac{9}{8} = -\frac{1}{\cancel{3}} \cdot \frac{\cancel{9}^3}{8} = -\frac{3}{8}$

b)  $2 \cdot \frac{1}{6} - \frac{3}{8} \cdot 4 = \frac{1}{3} - \frac{3}{2} = \frac{2-9}{6} = -\frac{7}{6}$

c)  $\frac{\frac{6}{7}-\frac{9}{14}}{\frac{8}{7}+\frac{6}{7} \cdot \frac{3}{2}} = \frac{\frac{12}{14}-\frac{9}{14}}{\frac{8}{7}+\frac{18}{14}} = \frac{\frac{3}{14}}{\frac{8}{7}+\frac{9}{7}} = \frac{\frac{3}{14}}{\frac{17}{7}} = \frac{3}{14} \cdot \frac{7}{17} = \frac{3}{14} \cdot \frac{\cancel{7}^1}{\cancel{17}^1} = \frac{1}{8}$

Uprav a rozlož na součin

d)  $49 - (-4a)^2 = 49 - 16a^2 = (7-4a)(7+4a)$

Zjednoduš

$2 \cdot 0,3 \cdot 0,5$

e)  $(0,3x+0,5)^2 = 0,09x^2 + 0,3x + 0,25$  BOREC:  $\text{altern: } (0,3x+0,5)(0,3x+0,5) = 0,09x^2 + 0,15x + 0,15x + 0,25 = 0,09x^2 + 0,3x + 0,25$  0,30x

f)  $n \cdot (2n-1) = (-2n-n) \cdot (3n+2) + (1-2n) \cdot (1+2n) = 2n^2 - n + 3n^2 + 6n + 1 - 4n^2 = 7n^2 + 5n + 1$  BOREC:  $n^2 - B^2$   
 $+ 3n \cdot (3n+2)$

Řeš rovnici:

g)  $\frac{2-x}{2} + 2x = 2,5x - 3 \quad / \cdot 2$

$2-x+4x = 5x-6$

$2+3x = 5x-6$

$3x-5x = -6-2$

$-2x = -8$

$x = 4$

$/: (-2)$

Řeš rovnici:

h)  $3 \cdot \frac{y+1}{2} - \frac{y}{3} = \frac{3}{2} \cdot \frac{2y-3}{2} + \frac{3}{2}$

$\frac{3y+3}{2} - \frac{y}{3} = \frac{2y-3}{2} + \frac{3}{2} \quad / \cdot 6$

$9y+9-2y = 6y-9+9$

$7y+9 = 6y$

$7y-6y = -9$

$y = -9$

### Test z aritmetiky 30

Cermat 2024 PAD (12b)

$$a) \left(2\frac{3}{2}\right) : \frac{1}{2} + \left(\frac{5}{6}\frac{3}{4}\right) : \frac{2}{3} = \frac{4}{3} \cdot \frac{2}{1} + \frac{10}{8} \cdot \frac{3}{2} = \frac{8}{3} + \frac{5}{3} = \frac{13}{3}$$

$$2 \cdot \frac{2}{3} = \frac{4}{3} \quad \frac{5}{6} \cdot \frac{4^2}{3} = \frac{10}{3}$$

$$b) \frac{\frac{13}{10} - 1,4}{\frac{2 \cdot 2}{2 \cdot 15} + \frac{1 \cdot 5}{6 \cdot 5}} = \frac{\frac{13}{10} - \frac{14}{10}}{\frac{4}{30} + \frac{5}{30}} = \frac{-\frac{1}{10}}{\frac{9}{30}} = -\frac{1}{10} \cdot \frac{3}{10} = -\frac{1}{10} \cdot \frac{10}{3} = -\frac{1}{3}$$

Rozlož na součin podle vzorce

$$c) 9a^2 - 16 = (3a - 4)(3a + 4)$$

$$d) \left(a - \frac{a}{4}\right)^2 = \left(\frac{4}{4}a - \frac{1}{4}a\right)^2 = \left(\frac{3}{4}a\right)^2 = \frac{9}{16}a^2$$

Zjednodušte a výsledek rozložte na součin vytýkáním.

$$e) (c-5) \cdot (2-3c) - (c-2c) \cdot 3c - c \cdot 7 = 2c - 3c^2 - 10 + 15c + 3c^2 - 7c = 10c - 10 = 10 \cdot (c-1)$$

Řeš rovnici:

$$f) -2 \cdot (x+4) - 3 \cdot (x+1)^2 = x \cdot (2-3x)$$

$$-2x - 8 - 3x^2 - 6x - 3 = 2x - 3x^2$$

$$-8x - 11 = 2x$$

$$-8x - 2x = 11$$

$$-10x = 11$$

$$x = -1,1$$

nebo

$$x = -\frac{11}{10}$$

Řeš rovnici:

$$g) 6 - \frac{3-2y}{5} \cdot 2 = 4y$$

$$6 - \frac{6-4y}{5} = 4y \quad / \cdot 5$$

$$30 - 6 + 4y = 20y$$

$$24 + 4y = 20y$$

$$4y - 20y = -24$$

$$-16y = -24 \quad / : (-8)$$

$$2y = 3$$

$$y = \frac{3}{2}$$

Test z aritmetiky 31

Cermat 2024 PBD (12b)

$$a) \left(\frac{3}{4} + \frac{4}{3}\right) \cdot \left(\frac{2}{3} - \frac{6}{5}\right) = \left(\frac{9+16}{12}\right) \cdot \left(\frac{10-18}{15}\right) = \frac{25}{12} \cdot \frac{-8}{15} = -\frac{5}{12} \cdot \frac{8}{3} = -\frac{10}{9}$$

$$b) \frac{\frac{5}{9} - \frac{3}{2} : \frac{3}{5}}{\frac{2}{3} + \frac{1}{6} - \frac{7}{12}} = \frac{\frac{5}{9} - \frac{3}{2} \cdot \frac{5}{3}}{\frac{8+2-7}{12}} = \frac{\frac{5}{9} - \frac{5}{2}}{\frac{3}{12}} = \frac{10-45}{18} = -\frac{35}{18} = -\frac{35}{18} \cdot \frac{1}{4} = -\frac{35}{18} \cdot \frac{1}{1} = -\frac{70}{9}$$

Zjednodušte

VZOREC:  $(-3-2x)^2 = 9 + 12x + 4x^2$       alt:  $(-3-2x)(-3-2x) = 9 + 6x + 6x + 4x^2 = 9 + 12x + 4x^2$

Uprav a rozlož na součin podle vzorce

$$d) 6400 - (x^2 - 3600) = 6400 - x^2 + 3600 = 10000 - x^2 = (100 - x)(100 + x)$$

Zjednoduš

VZOREC:  $(A+B)^2 - (2x^2 + 8x - 5x - 20)$

$$e) (3x+1)^2 - x \cdot 7x - (2x-5) \cdot (x+4) = 9x^2 + 6x + 1 - 7x^2 - 2x^2 - 8x + 5x + 20 = 3x + 21$$

alt:  $(3x+1)(3x+1) = 9x^2 + 3x + 3x + 1$  ↗

Řeš rovnici:

$$f) 1,6 : 2 - \frac{x}{2} = 3 \cdot 0,7x + 3,4$$

$$0,8 - \frac{x}{2} = 2,1x + 3,4 \quad /:10$$

$$8 - 5x = 21x + 34$$

$$-5x - 21x = 34 - 8$$

$$-26x = 26 \quad /:(-26)$$

$$x = -1$$

Řeš rovnici:

$$g) \frac{5-2y}{3} + \frac{y}{9} = \frac{3-y}{6} \quad /:18$$

$$30 - 12y + 2y = 9 - 3y$$

$$30 - 10y = 9 - 3y$$

$$-10y + 3y = 9 - 30$$

$$-7y = -21 \quad /:(-7)$$

$$y = 3$$

Test z aritmetiky 32

Cermat 2024 PCD (12b)

$$a) \frac{2 \cdot 7}{2 \cdot 5} + 3,3 - \frac{1 \cdot 5}{2 \cdot 5} = \frac{14}{10} + \frac{33}{10} - \frac{5}{10} = \frac{42}{10} = \frac{21}{5} : \frac{2}{5} = \frac{21}{5} \cdot \frac{5}{2} = \frac{21}{2}$$

$$\rightarrow \frac{21}{5} \cdot \frac{5}{2}$$

$$b) \left( \frac{1}{2} + \frac{1}{3} \cdot \frac{5}{6} \right) - \frac{7}{2} + \frac{3}{5} : \frac{3}{2} - 1 = \left( \frac{5}{10} + \frac{4}{10} \right) - \frac{7 \cdot 5}{2 \cdot 5} + \frac{2 \cdot 3}{5 \cdot 2} - 1 = \frac{9}{10} - \frac{35}{10} + \frac{4}{10} - \frac{10}{10} = -\frac{32}{10} = -\frac{16}{5}$$

$$\frac{1}{2} \cdot \frac{6}{5} = \frac{2}{5} = \frac{4}{10}$$

Zjednodušte

$$c) \left( \frac{b}{3} - 3b \right)^2 = \left( \frac{b}{3} - \frac{9b}{3} \right)^2 = \left( -\frac{8}{3}b \right)^2 = \frac{64}{9}b^2$$

Uprav a rozlož na součin podle vzorce

$$d) 5 - (1 - x^2) - x \cdot 2x = 5 - 1 + x^2 - 2x^2 = 4 - x^2 = (2 - x)(2 + x)$$

Zjednoduš

$$e) (c-7) \cdot (c-7) - (c-5) \cdot 3c + c \cdot \frac{2c}{c+c} = c^2 - 7c - 7c + 49 - 3c^2 + 15c + 2c^2 = c + 49$$

Řeš rovnici:

$$f) \left( x + \frac{1}{2}x \right) \cdot 2 = \left( x + \frac{1}{6}x \right) \cdot 2 + 6$$

$$2 \cdot \frac{1}{6}x = \frac{1}{3}x$$

$$2x + x = 2x + \frac{1}{3}x + 6 \quad /:3$$

$$6x + 3x = 6x + x + 18$$

$$9x = 7x + 18$$

$$9x - 7x = 18$$

$$2x = 18 \quad /:2$$

$$x = 9$$

Řeš rovnici:

$$g) \frac{1}{2} \cdot (x+2) - (x-2)^2 = 6 - x^2$$

$$\frac{1}{2}x + 1 - x^2 + 4x - 4 = 6 - x^2 \quad /:2$$

$$x + 2 + 8x - 8 = 12$$

$$9x - 6 = 12$$

$$9x = 12 + 6$$

$$9x = 18 \quad /:9$$

$$x = 2$$

Test z aritmetiky 33

Cermat 2024 PDD (12b)

$$\ominus : \ominus \rightarrow \oplus$$

$$\text{a)} \frac{\left(\frac{1}{6} - \frac{1}{3}\right) : \left(-\frac{5}{3}\right)}{0,3} = \frac{\left(\frac{1}{6} - \frac{2}{6}\right) : \left(-\frac{5}{3}\right)}{\frac{3}{10}} = \frac{-\frac{1}{6} : \left(-\frac{5}{3}\right)}{\frac{3}{10}} = \frac{\frac{1}{6} \cdot \frac{3}{5}}{\frac{3}{10}} = \frac{\frac{1}{10}}{\frac{3}{10}} = \frac{1}{10} \cdot \frac{10}{3} = \frac{1}{3}$$

$$\text{b)} \frac{1}{6} + \frac{1}{3} \cdot \left(\frac{2}{5} - 1\right) = \frac{1}{6} + \frac{1}{3} \cdot \left(-\frac{3}{5}\right) = \frac{1}{6} - \frac{1}{3} \cdot \frac{3}{5} = \frac{5}{30} - \frac{6}{30} = -\frac{1}{30}$$

$$\frac{2}{5} - \frac{5}{5}$$

Zjednodušte

$$\text{c)} \left(\frac{1}{3} - 4b\right)^2 = \frac{1}{9} - \frac{8}{3}b + 16b^2 \quad \text{altor: } \left(\frac{1}{3} - 4b\right)\left(\frac{1}{3} - 4b\right) = \frac{1}{9} - \frac{4}{3}b - \frac{4}{3}b + 16b^2 = \frac{1}{9} - \frac{8}{3}b + 16b^2$$

Uprav a rozlož na součin.

$$\text{d)} a \cdot (-a) - 2^2 \cdot 3a + 6a^2 = -a^2 - 12a + 6a^2 = 5a^2 - 12a = a \cdot (5a - 12)$$

Zjednoduš

$$\text{e)} (2x+3)^2 - x \cdot 6 - 4 \cdot (x-1)^2 = 4x^2 + 12x + 9 - 6x - 4(x^2 - 2x + 1) = 4x^2 + 12x + 9 - 6x - 4x^2 + 8x - 4 = 14x + 5$$

Řeš rovnici:

$$\text{f)} x - \frac{x-2}{2} = \frac{2x}{3} - 2 \quad / \cdot 6$$

$$6x - 3x + 6 = 4x - 12$$

$$3x + 6 = 4x - 12$$

$$3x - 4x = -12 - 6$$

$$-x = -18 \quad / : (-1)$$

$$x = 18$$

Řeš rovnici:

$$\text{g)} 2 \cdot (3x - 2,5) = -5 + 3 \cdot (3x - 2)$$

$$6x - 5 = -5 + 9x - 6$$

$$6x - 5 = 9x - 11$$

$$6x - 9x = -11 + 5$$

$$-3x = -6 \quad / : (-3)$$

$$x = 2$$



Test z aritmetiky 35

Cermat 2025 PBD (11b)

a)  $\left(\frac{11}{5} - \frac{11}{6}\right) : \left(-\frac{1}{3}\right) = \left(\frac{66-55}{30}\right) : \left(-\frac{1}{3}\right) = \frac{11}{30} : \left(-\frac{1}{3}\right) = -\frac{11}{30} \cdot \frac{3}{1} = -\frac{11}{10}$

b)  $\frac{20 - \sqrt{4 \cdot 3^2}}{3 \cdot \sqrt{100 - 64}} : \frac{4+3}{4 \cdot 3} = \frac{20 - 2 \cdot 3}{3 \cdot 6} : \frac{7}{12} = \frac{14}{18} \cdot \frac{12}{7} = \frac{4}{3}$   
*alt:  $-\sqrt{36} = -\sqrt{36} = -6$   
 $\rightarrow$  odmocnujeme součin*

Uprav a rozlož na součin

e)  $(2k)^2 - k \cdot (1+2k) = 4k^2 - k - 2k^2 = 2k^2 - k = k \cdot (2k - 1)$

Zjednoduš

*POREČ:*  
 $-(x^2 - 6x + 9)$

d)  $x \cdot 3x - 2x \cdot 3 - (x-3)^2 = 3x^2 - 6x - x^2 + 6x - 9 = 2x^2 - 9$

alt:  $-(x-3)(x-3) = -(x^2 - 3x - 3x + 9) = -x^2 + 6x - 9$

e)  $7a \cdot (a+3) + 2 \cdot (1-3a) \cdot (a+5) = 7a^2 + 21a + 2a + 10 - 6a^2 - 30a = a^2 - 7a + 10$

*1)  $(2-6a) \cdot (a+5)$*

*2)  $2 \cdot [a+5-3a^2-15a]$*

Řeš rovnici:

f)  $\frac{7}{12}x + 2 \cdot \left(\frac{3}{8}x - 1\right) = -3 \cdot \left(\frac{x}{9} + 1\right)$

$\frac{7}{12}x + \frac{3}{4}x - 2 = -\frac{x}{3} - 3 \quad / \cdot 12$

$7x + 9x - 24 = -4x - 36$

$16x - 24 = -4x - 36$

$16x + 4x = -36 + 24$

$20x = -12 \quad / : 4$

$5x = -3$

$x = -\frac{3}{5} \quad \text{nebo} \quad x = -0,6$

Řeš soustavu rovnic:

g)  $6x + y = 14$   
 $3x + 2y = 1 \quad / \cdot (-2)$

*1)  $6x + y = 14$   
 $-6x - 4y = -2$   
 $-3y = 12 \quad / : (-3)$   
 $y = -4$*

$3x + 2 \cdot (-4) = 1$

$3x - 8 = 1$

$3x = 1 + 8$

$3x = 9 \quad / : 3$

$x = 3$

*$\rightarrow y = 14 - 6x$*

*$3x + 2 \cdot (14 - 6x) = 1$*

*$3x + 28 - 12x = 1$*

*$-9x = 1 - 28$*

*$-9x = -27 \quad / : (-9)$*

*$x = 3$*

*$y = 14 - 6 \cdot 3$*

*$y = -4$*

Test z aritmetiky 36

Cermat 2025 PCD (11b)

a)  $\frac{\sqrt{10^2 - 19}}{\sqrt{10^2}} = \frac{\sqrt{100 - 19}}{\sqrt{100}} = \frac{\sqrt{81}}{10} = \frac{9}{10}$

b)  $\frac{\left(\frac{3}{5}\right)^2}{\frac{27}{34} \cdot \left(\frac{2}{3} - \frac{3^2}{5}\right)} = \frac{\frac{9}{25}}{\frac{27}{34} \cdot \left(\frac{2}{3} - \frac{9}{5}\right)} = \frac{9}{25} \cdot \frac{34}{27} \cdot \frac{15}{5} = \frac{9}{25} \cdot \frac{34}{9} \cdot \frac{15}{5} = \frac{34}{25} \cdot \frac{15}{5} = \frac{34}{5} \cdot \frac{3}{1} = \frac{102}{5}$

$\hookrightarrow \frac{2}{3} - \frac{9}{5} = \frac{10 - 27}{15} = -\frac{17}{15}$

$\hookrightarrow$  altern:  $(8a-4)(8a-4) = 64a^2 - 32a - 32a + 16 = 64a^2 - 64a + 16$

Zjednoduř

VřOREC:

e)  $(4+8a-8)^2 = (8a-4)^2 = 64a^2 - 64a + 16$

d)  $(2-3x) \cdot 2 + (2x)^2 - x \cdot (-6) = 4 - 6x + 4x^2 + 6x = 4 + 4x^2$

VřOREC:  $\hookrightarrow$  altern:  $(1-2n)(1+2n) = 1+2n-2n-4n^2$

e)  $(1-2n) \cdot (1-2n+4n) - 2n \cdot (1-3n) + (3n-1) = 1-4n^2 - 2n + 6n^2 + 3n - 1 = 2n^2 + n$

Řeř rovnici:

f)  $5x + \frac{2}{15} + \frac{1}{15}x = \frac{2}{3}x - \frac{3}{5} \quad / \cdot 15$

$75x + 2 + x = 10x - 9$

$75x + x - 10x = -9 - 2$

$66x = -11 \quad / : 11$

$6x = -1$

$x = -\frac{1}{6}$

Řeř rovnici:

g)  $4 - \frac{7-3y}{5} = 3 + \frac{7y-4}{10} \quad / \cdot 10$

$40 - 14 + 6y = 30 + 7y - 4$

$26 + 6y = 26 + 7y$

$6y - 7y = 26 - 26$

$-y = 0$

$y = 0$

Test z aritmetiky 37  
Cermat 2025 PDD (11b)

$$a) \left(\frac{7}{5} - \frac{7}{4}\right) \cdot \frac{2}{5} = \left(\frac{28-35}{20}\right) \cdot \frac{2}{5} = \frac{-7}{20} \cdot \frac{2}{5} = -\frac{7}{20} \cdot \frac{2}{5} = -\frac{7}{50} = -\frac{7}{8}$$

$$b) \frac{\left(1 + \frac{1}{7}\right)^2 \cdot \frac{7}{4}}{\sqrt{25} - \frac{3^2}{5}} = \frac{\left(\frac{7}{7} + \frac{1}{7}\right)^2 \cdot \frac{7}{4}}{5 - \frac{9}{5}} = \frac{\left(\frac{8}{7}\right)^2 \cdot \frac{7}{4}}{\frac{25}{5} - \frac{9}{5}} = \frac{\frac{64}{49} \cdot \frac{7}{4}}{\frac{16}{5}} = \frac{\frac{16}{7} \cdot \frac{7}{4}}{\frac{16}{5}} = \frac{16}{7} \cdot \frac{5}{16} = \frac{5}{7}$$

Uprav a rozlož na součin

$$c) k \cdot (k-9) + 9 \cdot (k-16) = k^2 - 9k + 9k - 144 = k^2 - 144 = (k-12)(k+12)$$

Zjednoduš

$$d) (y+1)^2 + (y-1) \cdot 2y = y^2 + 2y + 1 + 2y^2 - 2y = 3y^2 + 1$$

$$e) (x-15) \cdot (2x-x) - (5x-8) \cdot (-3+1) - 1 = x^2 - 15x + 10x - 16 - 1 = x^2 - 5x - 17 + 2 \cdot (5x-8)$$

Řeš rovnici:

$$f) 0,1x + 5 \cdot (0,04x - 3,2) = 4 - 0,7x$$

$$\begin{aligned} 0,1x + 0,2x - 16 &= 4 - 0,7x & / \cdot 10 \\ x + 2x - 160 &= 40 - 7x \\ 3x + 7x &= 40 + 160 \\ 10x &= 200 \\ x &= 20 \end{aligned}$$

g) Řeš soustavu rovnic:

$$\begin{aligned} 3x - (y+1) &= 10 \\ 2x - 9 &= y & \text{dosaž.} \\ 3x - y - 1 &= 10 \\ 3x - (2x - 9) - 1 &= 10 \\ 3x - 2x + 9 - 1 &= 10 \\ x + 8 &= 10 \\ x &= 2 \\ y &= 2 \cdot 2 - 9 \\ y &= -5 \end{aligned}$$

11.2p

$$\begin{aligned} 3x - y - 1 &= 10 \\ 2x - y &= 9 & / \cdot (-1) \\ \hline 3x - y &= 11 \\ -2x + y &= -9 \\ \hline x &= 2 \\ -4 + y &= -9 \\ y &= -5 \end{aligned}$$

Test z aritmetiky 38  
Cermat 2026 PID (13b)

a)  $-5 \cdot 5 + (-12)^2 - 13^2 = -25 + 144 - 169 = -50$

b)  $\sqrt{1-0,8^2} : 6 = \sqrt{1-0,64} : 6 = \sqrt{0,36} : 6 = 0,6 : 6 = 0,1$

c)  $\frac{3 \cdot 5}{3 \cdot 24} + \frac{5 \cdot 7}{24 \cdot 3} = -\frac{15}{72} + \frac{35}{72} = \frac{20}{72} = \frac{10}{36} = \frac{5}{18}$

d)  $\frac{\left(\frac{125}{21} \cdot \frac{7^4}{25} - 9\right) : 4}{11} = \frac{\left(\frac{5}{3} - \frac{27}{3}\right) : 4}{11} = \frac{\left(-\frac{22}{3}\right) \cdot \frac{1}{4}}{11} = -\frac{\frac{11}{6}}{11} = -\frac{11}{6} : 11 = -\frac{11}{6} \cdot \frac{1}{11} = -\frac{1}{6}$

Upravte a rozložte na součin

e)  $3y \cdot (x+3y) - y = 3xy + 9y^2 - y = y \cdot (3x + 9y - 1)$

f)  $n \cdot (9n-1) + n - 4 = 9n^2 - n + n - 4 = 9n^2 - 4 = (3n+2)(3n-2)$

Zjednodušte

g)  $4 \cdot (2x \cdot x - x) - 3 + (2x+1)(3-4x) = \underline{8x^2} - 4x - 3 + 6x - 8x^2 + 3 - 4x = -2x$

Řeš rovnici:

h)  $3 \cdot \left(4 - \frac{3}{4}x\right) + x = 1 - \frac{5}{4}x$

$12 - \frac{9}{4}x + x = 1 - \frac{5}{4}x \quad / \cdot 4$

$48 - 9x + 4x = 4 - 5x$

$48 - 5x = 4 - 5x$

$-5x + 5x = 4 - 48$

$0 = -44$

ROVNICE NEMÁ ŘEŠENÍ

i) Řeš soustavu rovnic:

$2x - y = 7 \quad / \cdot (-2)$   
 $x - 2y = 11$

$-4x + 2y = -14$   
 $x - 2y = 11$

$-3x = -3$

$x = 1$

$2 - y = 7$

$-y = 7 - 2$

$-y = 5 \quad / \cdot (-1)$

$y = -5$

$\leftarrow$  II. zp  
 $\rightarrow x = 11 + 2y$

$2 \cdot (11 + 2y) - y = 7$

$22 + 4y - y = 7$

$3y = 7 - 22$

$3y = -15 \quad / : 3$

$y = -5$

$x = 11 + 2 \cdot (-5)$

$x = 11 - 10$

$x = 1$